



Improved Pulse Detection from Head Motions Using DCT

Irani, Ramin; Nasrollahi, Kamal; Moeslund, Thomas B.

Published in:

Proceedings of the 9th International Conference on Computer Vision Theory and Applications

DOI (link to publication from Publisher):

[10.5220/0004669001180124](https://doi.org/10.5220/0004669001180124)

Publication date:

2014

Document Version

Early version, also known as pre-print

[Link to publication from Aalborg University](#)

Citation for published version (APA):

Irani, R., Nasrollahi, K., & Moeslund, T. B. (2014). Improved Pulse Detection from Head Motions Using DCT. In S. Battiato, & J. Braz (Eds.), *Proceedings of the 9th International Conference on Computer Vision Theory and Applications* (Vol. 3, pp. 118-124). Institute for Systems and Technologies of Information, Control and Communication. <https://doi.org/10.5220/0004669001180124>

General rights

Copyright and moral rights for the publications made accessible in the public portal are retained by the authors and/or other copyright owners and it is a condition of accessing publications that users recognise and abide by the legal requirements associated with these rights.

- Users may download and print one copy of any publication from the public portal for the purpose of private study or research.
- You may not further distribute the material or use it for any profit-making activity or commercial gain
- You may freely distribute the URL identifying the publication in the public portal -

Take down policy

If you believe that this document breaches copyright please contact us at vbn@aub.aau.dk providing details, and we will remove access to the work immediately and investigate your claim.

Improved Pulse Detection from Head Motions Using DCT

Ramin Irani, Kamal Nasrollahi and Thomas B. Moeslund
Visual Analysis of People Laboratory, Aalborg University (AAU)
Sofieendalsvej 11, 9200 Aalborg, Denmark
{mah, kn, tbm}@create.aau.dk

Keywords: Heartbeat rate, Head motion detection, Trajectory, Feature point tracker, Principle component analysis, Discrete cosine transforms, Electrocardiogram

Abstract: The heart pulsation sends out the blood throughout the body. The rate in which the heart performs this vital task, heartbeat rate, is of curial importance to the body. Therefore, measuring heartbeat rate, a.k.a. pulse detection, is very important in many applications, especially the medical ones. To measure it, physicians traditionally, either sense the pulsations of some blood vessels or install some sensors on the body. In either case, there is a need for a physical contact between the sensor and the body to obtain the heartbeat rate. This might not be always feasible, for example, for applications like remote patient monitoring. In such cases, contactless sensors, mostly based on computer vision techniques, are emerging as interesting alternatives. This paper proposes such a system, in which the heartbeats (pulses) are detected by subtle motions that appear on the face due to blood circulation. The proposed system has been tested in different facial expressions. The experimental results show that the proposed system is correct and robust and outperforms state-of-the-art.

1 INTRODUCTION

Heartbeat rate is obviously a vital sign of human body's activity and its measurement is of great importance in many applications, for instance, fitness assessment, training programs and medical diagnosis. For example, in fitness assessment during the exercise, heartbeat rate is used as a crucial sign that helps to assess the condition of cardiovascular system. Here it can be used also for ensuring the safety of the process. If the heartbeat rate goes beyond the normal range, continuing the exercise is not safe any longer.

Heartbeat rate is usually measured by devices that take samples of heartbeats and compute the beats per minute (bpm). Currently, one of the popular non-invasive and standard devices for measuring the heartbeat rate is electrocardiogram (ECG). They are very accurate, but expensive. These devices are electrode-based and therefore require wearing adhesive gel patches or chest straps that may cause skin irritation and slight pain. Commercial pulse oximetry sensor is another technique that is placed on specific parts of body like fingertips or earlobe.

Though the above mentioned devices are accurate, they are inconvenient as they need to have physical contact with patient's body. Therefore, developing contactless methods, which are based on the patient's physiological signals, have recently been considered as an interesting alternative for measuring heartbeat rate. This technology would also decrease the amount of cabling and clutter related to Intensive Care Unit (ICU) monitoring, long-term epilepsy monitoring, sleep studies, and any continues heartbeat rate measurement (Poh, 2008). These contactless methods that are usually based on computer vision techniques can be divided into two groups. In the first group, known as *photoplethysmography* (PPG) methods, usually a red, or an infrared light is transmitted on the patients (face or body) and the reflected light is sensed by the system. The variations in the transmitted and the reflected lights are then used to measure heartbeat rate. Besides using dedicated light sources, the main drawbacks of PPG systems are that they are susceptible to motion artefact (Verkruysse, 2008, Humphreys, 2007, Takano, 2007, Hu, 2008, Wieringa, 2005).

In the second group of computer vision based methods there is no need for a dedicated light source. These methods assume that the periodic circulation of the blood by the heart to the rest of the body, including the head, generates some periodic subtle changes to the skin color of the face and also generates some subtle head motions. These motions are not usually visible to naked eyes but they can be viewed by techniques like, for example, Eulerian video magnification (Wu, 2012). These periodic changes to the skin colors and head motions are then utilized to measure heartbeat rate. For example, in (Poh, 2010) periodic changes in the skin color of the face has been used for this purpose. In this system (Poh, 2010) face image of the subject is first found, by a simple camera. Then, it is separated into its colour channels and each channel is tracked independently. For each of these tracked colour channels, a trajectory is found. Then, all the trajectories are fed to an Independent Component Analysis (ICA) algorithm. The output of ICA, presents independent sources that have caused changes to the skin colour of the face. Then, it is assumed that the most periodic output of ICA should be generated by the most periodic source that is present on the face, i.e., heartbeat. This system is effective, but it suffers from sensitivity to skin color and noise. It means, if the skin is not detected properly, or if the captured facial video is noisy, the system does not provide accurate results.

To overcome the sensitivity to noise and skin detection of system (Poh, 2010), very recently in (Balakrishnan, 2013) a motion-based contactless system for measuring heartbeat rate was introduced. As mentioned above, this method is based on the fact that periodic circulation of the blood from the heart to the body, including the head through the aorta and carotid arteries, causes the head to move in a cyclic motion (Wu, 2012). Similar to (Poh, 2010), this system also uses a simple camera for recording facial images of patients. Having detected the face, they extracted vertical component of head motion by tracking feature points, and generate some trajectories for each feature point. These trajectories are then filtered by a Butterworth filter to remove the irrelevant frequencies. Next on the contrary (Poh, 2010) they use Principle Component Analysis (PCA) (instead of ICA) to decompose the filtered trajectories into a set of source signals. Then, they use the same assumption as (Poh, 2010), that the most periodic signal is generated by the most periodic source of the motion that is present in the face, i.e., by heartbeat. To find the periodicity of the outputs of PCA, they apply Fast Fourier Transform

(FFT) to the trajectories, and use the percentage of total spectral power of the signal accounted for by the frequency with the maximal power and its first harmonic (Balakrishnan, 2013).

This method gives reasonable results when the face is frontal and does not move. Our experiment shows that involuntary motion and facial expression causes dramatic effect on the accuracy of this system. Furthermore, as mentioned above, this system is based on using the frequency with maximal power as the first harmonic of the estimated heartbeat rate. But, this assumption is not always true, especially when the facial expression is changing. The proposed system in this paper improves the system of (Balakrishnan, 2013) by replacing the FFT with a Discrete Cosine Transform (DCT). Furthermore, we show that involving a moving average filter before the Butterworth filter improves the results. It is shown that the proposed system outperforms the system of (Balakrishnan, 2013), significantly.

The rest of this paper is organized as follows: The clear problem statement and the contributions of the proposed system are given in the next section. Section 3 explains the employed methodology of the proposed system. The experimental results are reported in Section 4. Finally, the paper is concluded in Section 5.

2 PROBLEM STATEMENT AND MAIN CONTRIBUTION

The proposed system in this paper develops a vision-based contactless algorithm for heartbeat rate measurement using the assumption that periodic blood circulation by the heart to the head generates subtle periodic motion on the face. The proposed system is based on the very recent work of (Balakrishnan, 2013), but it advances this work by:

- 1) Replacing the FFT of the system of (Balakrishnan, 2013) by a DCT, and
- 2) Using a moving average filter before the Butterworth filter that is employed in (Balakrishnan, 2013).

The proposed modifications are simple, but are shown to be very effective. The results of the proposed system are:

- 1) More correct compared to the results of the system of (Balakrishnan, 2013) when they are compared to the ground truth data.

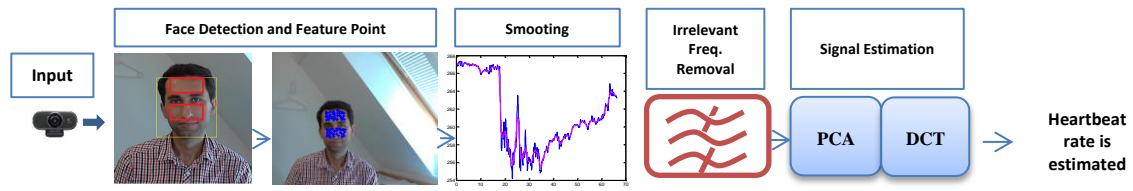


Figure 1: The block diagram of the proposed system

2) More robust than the results of the system of (Balakrishnan, 2013) when the face is moving or facial expression is changing.

3 METHODOLOGY

The block diagram of the proposed system is shown in Figure 1. As it can be seen from this figure, the subject is continuously filmed by a Logitech webcam with a resolution of 640x480 pixels. Then, the subject's face is detected by Viola and Jones (Viola, 2001) face detector. From the detected faces, the regions of interest of our system, and consequently the feature points are extracted and tracked by the Lucas Kanade's algorithm (Bouguet, 2000). Then, a moving average filter and a band pass filter are applied to the vertical component of the trajectories of each feature point to remove extraneous frequencies and involuntary head motions. Then, the filtered trajectories are fed to PCA to find the strongest independent components. Among these components, the most periodic one belongs to heartbeat. To find this most periodic one, we apply DCT to all the components obtained by PCA. Each of these sub-blocks is explained in the following subsections.

3.1 Face Detection

Locating the face in the scene refers to identifying a region containing a human face. Viola and Jones algorithm (Viola, 2001) has been employed for this purpose which is based on Haar-like rectangular features that are extracted from integral images. This detector is fast and efficient, but it fails to detect rotated faces and those which are of poor quality. However, it works fine for the purposes of the proposed system.

The regions detected by the Viola and Jones detector cannot be directly used in our system, as it contains the areas of eyes and the mouth which are not good for the purposes of our system. Because these areas are the most changeable areas of the face, and they may change very much by any

changes in facial expression, eye blinking, etc. Therefore, the trajectories obtained from these changeable will not reflect the motion caused by heartbeat. Instead, they reflect the motion caused by the changes in their own positions due to the changes in the facial expression. Tracking these sensitive regions therefore does not produce stable results. The most stable parts of the face, which are robust against changes in the facial expressions, are the forehead and the area around the nose. To keep these regions, we first keep 50% (experimentally obtained) of the width and 70% (experimentally obtained) of the height of the region that is detected the Viola and Jones's face detector. Then, in this refined region we remove the area of the eyes, by removing all the pixels that are located in the range of 25% to 45% (experimentally obtained) of the height of the refined region (Figure 2).

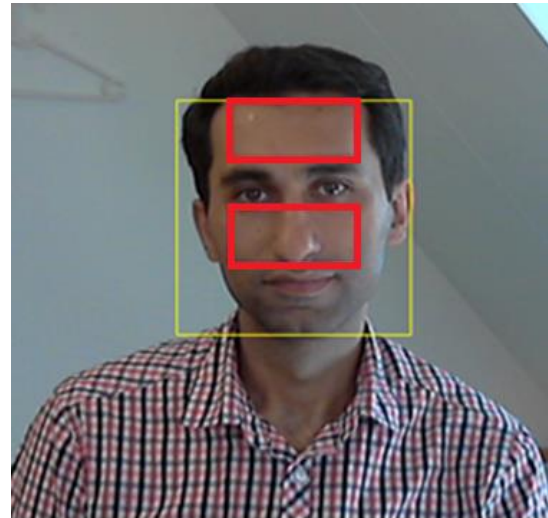


Figure 2: The yellow box is returned by the Viola and Jones face detector and the red boxes are those that are of the interest of the proposed system.

3.2 Feature Points selection

Having detected the regions of interest in the previous sub-block of the system, in this step they are fed to the *Good Feature Tracking algorithm* of (Shi, 1994) to select the feature points. This

algorithm is based on finding and tracking the corners. To do so, it calculates the minimal eigenvalue of every point in our previously kept regions of the face and rejecting corners with minimal eigenvalues. Then, it goes through the strongest corners and removes those features that are too close the stronger features (Shi, 1994). To increase the efficiency of this system, it is suggested in (Balakrishnan, 2013) to divide the sub-regions obtained from Viola and Jones detector into smaller areas to achieve uniform selected regions. Therefore, we have adopted this idea here.

3.3 Trajectory Generation and Smoothing

To extract the motion trajectory signals from the selected feature points in the previous subsection, we have used Lucas Kanade's algorithm (Bouquet, 2000) to obtain x and y components of feature points inside our previously extracted regions of interest in each frame. Since the very tiny motions of the head, which are the basis for calculating the heartbeat rate in this work, are due to the blood circulation through aorta towards head (obviously in a vertical direction), we only consider the y components of the trajectories of the feature points in each frame.

The head motions are not only due to heartbeats (transferred to the head by aorta), but may appear for several reasons, for example, respiration, vestibular activity, facial expression, speaking and so on. To decrease the effects of the other sources, which cause quite large motions, a moving average filter is applied to the trajectories to smooth it (Figure 3). This will be further explained in the experimental results.

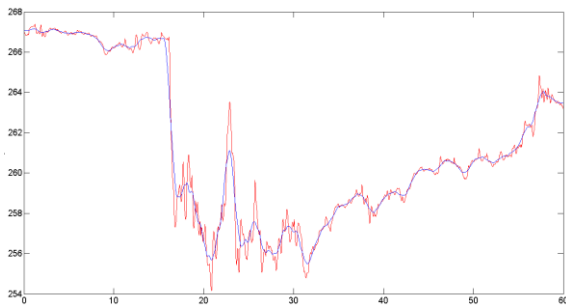


Figure 3: The effect of the employed moving average filter on the y components of the trajectory of one of the tracked feature points of one of the test subjects. The red and the blue signals are the original and the filtered signals, on the x axis of the above graph is the time and on the y axis is the y position of the tracked feature point over time.

Then, to remove the irrelevant frequencies (any frequency which might not be generated by the heartbeat) a pass band filter (an 8th order Butterworth filter) with cutoff frequency interval of [0.75 5] Hz has been applied to the obtained trajectory (Balakrishnan, 2013).

3.4 Signal Estimation

As mentioned above, the head motions are originated from different sources and only the one caused by the blood circulation through aorta is reflecting the heartbeat rate. To separate the sources of head motions, we have applied a PCA algorithm to the obtained trajectories. PCA converts the given trajectories into a set of linearly uncorrelated basis, i.e., the principal components.

Having separated the sources using PCA, the next step is to find the signal that has been generated by the heartbeat. Following (Balakrishnan, 2013) such a signal will be the most periodic signal. To quantify the signal periodicity we have utilized DCT as opposed to the system of (Balakrishnan, 2013) which have used FFT. Having applied DCT, we only keep those DCT components that carry the most significant power of the signal. To do so, we use the following algorithm:

- For the trajectory of the i th feature points, $i \in [1..N]$, S_i :
 - Calculate the DCT of the i th trajectory and obtain SC_i
 - Determine $\{K_j\}_i$ which is the set of indexes for $\{S_i(t)\}$ such that K_j is the index of the M first highest power components into SC_i which consists 50% of power of S_i ,
 - $j \in [1..M_i]$ (M_i is number of components which carry 50% of total power of S_i)
 - Determine $\{Kh_l\}_i$ which is the set of the first 5 smallest index into $\{K_j\}_i$ for each S_i such that $2 \times Kh_l$ be found on SC_i
 - $l = 1:5$.
 - The periodicity of the signal can be obtained by:

$$Q_i = \frac{\text{norm}[SC(Kh_l), SC(2 \times Kh_l)]}{\text{norm}[SC_i]}$$
- S_i with largest Q_i is the heartbeat rate signal, and the heartbeat rate can be obtained as: $\text{FFT}(\text{IDCT}(\min\{Kh_i\})) \times 60$ bpm

The effect of the above DCT-based algorithm for finding the heartbeat rate and its advantage over the

FFT of (Balakrishnan, 2013) has been shown in the experimental results.

4 EXPERIMENTAL RESULTS

The proposed approach has been implemented in Matlab R2013a. To be able to compare our system against state-of-the-art Balakrishnan et al.'s work (Balakrishnan, 2013) we have recorded the actual heartbeat rates of the test subjects by a Shimmer wireless ECG (Electrocardiogram) sensor. This sensor records and sends the ECG signals, to a remote computer as a data file. Figure 4 (top) shows a typical data that has been captured by this sensor. The FFT of this signal is shown in Figure 4 (bottom). It can be seen from this figure, that the FFT has 4 peaks on the frequencies 1.08, 2.14, 3.13, and 4.22. These show that most of the power of the recorded heartbeat signal is carried by these 4 component frequencies which seem to be approximately integer multiple components of $f_0 = 1.08 \text{ Hz}$, as a fundamental frequency or first harmonic. Therefore, we can conclude that period of the heartbeat signal per minute is $1.08 \times 60 = 64.8$. The numbers of pulses on Figure 4 (bottom) prove this.

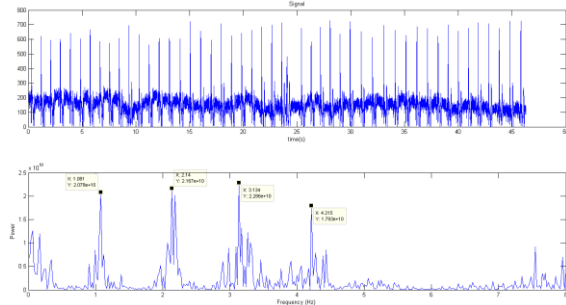


Figure 4: Recorded ECG signal and its FFT corresponding signals which shows the periodicity of the ECG signal.

Having shown that the ECG signals obtained by the employed sensor are indeed periodic (Figure 4), we now first explain the testing scenarios in which our data have been recorded. Then, we show the effects of the modifications that we have applied to the system of (Balakrishnan, 2013). Next, we give the details of the comparison of our system against the Balakrishnan et al.'s work (Balakrishnan, 2013).

4.1 Testing Scenarios

Five test subjects were asked to participate in testing the systems from which 32 different videos were

recorded. These videos are recorded by a Logitech webcam at a frame rate of 30 fps in different facial expressions and head poses. These are the situations in which the videos have been recorded in:

- Subjects look directly into the camera without changing their facial expressions (This is the same imaging condition as the system of (Balakrishnan, 2013)).
- Subjects turn around their faces from left (-180°) to right ($+180^\circ$) and look at seven different targets that are located at the same distance from each other.
- Subjects show smiling/laughing expression.
- Subjects repeat a given sentence.
- Subjects show angry expression.

The duration of each video is around 60 seconds.

4.2 The moving average filter and DCT

Before obtaining the periodicity of the selected source signal (Figure 1 block diagram), the only difference between our system and the work of (Balakrishnan, 2013) is that we have introduced a moving average filter. This does not have much effect when the face is standing still, and is facing the camera. But, as soon as the subject is changing his/her head pose and/or facial expressions are changing, there will be so many occlusions in the tracking of the feature points, that without using a moving average filter the results will be erroneous. Comparing Figure 5 (top) to Figure 5 (bottom) shows that including this moving average filter causes the employed PCA to pick a much smoother signal as the strongest component compared to the case where such a filter has not been included (Balakrishnan, 2013). This will gives us better results, for estimating the heartbeat rates, in the final step of the system.

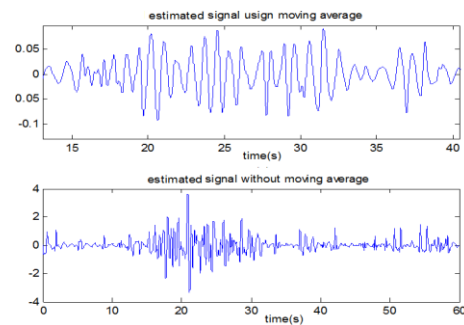


Figure 5: Comparing the estimated heartbeat rate signal when the moving average filter is used (top) and when it is not used (bottom).

Besides introducing the moving average filter for smoothing the estimated signal, in our system we have used DCT to estimate the periodicity of the estimated signal. The effect of this decision and comparing it with the FFT of (Balakrishnan, 2013) is shown in Figure 6. In this figure (top and middle parts) a signal and its FFT representation are shown. The maximum power of this FFT (3.603) gives a heartbeat rate of $3.603 \times 60 = 216.18$, while the actual heartbeat rate in this case is 60 bpm which can be estimated much better using the first harmonic ($1.001 \times 60 = 60.06$). Therefore, the total spectral power of the signal and then using the maximal power and its first harmonic as have been used in (Balakrishnan, 2013) does not always produce the desired results. Instead, by using DCT in Figure 6 (bottom) it can be seen that a much better result will be obtained, if the component number 20 is selected as the component which carries the power of pulse frequency. Feeding this value of this component in the algorithm of section 3.4 results in an estimated beat rate of 60.88 bpm, which is very close to the actual value.

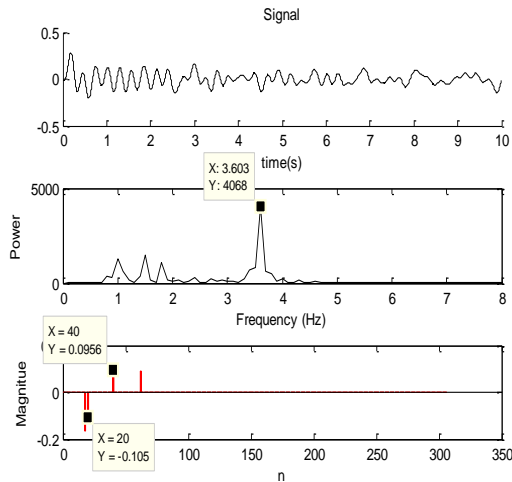


Figure 6: Extracting the beat rate of the signal (top) using the algorithm of (Balakrishnan, 2013) (middle) and our employed DCT (bottom).

4.3 Detailed Experiments

The proposed system has been compared against the state-of-the-art work of (Balakrishnan, 2013) using the testing data that was recorded in the previously explained testing scenarios. The results of comparing these systems (the proposed system and the work of (Balakrishnan, 2013) against the ground truth data obtained by the Shimmer ECG sensor for

the case which the testing subjects are looking directly into the camera are shown in Table 1. In this table, (a) is the subject number, (b) is the ground truth data read by a Shimmer ECG device, (c) is the heartbeat rate estimated by the system of (Balakrishnan, 2013), (d) is the error of the method of (Balakrishnan, 2013), (e) is the heartbeat rate estimated by our proposed method, (f) is the error of our proposed method. It can be seen that the error of our system is generally better than that of (Balakrishnan, 2013).

Table 1: The proposed system against system of (Balakrishnan, 2013), please see the text for descriptions of the headings.

a	b	c	d	e	f
S1-1	61.71	63.06	1.35	62.1	0.39
S1-2	66.67	67.04	0.37	67.03	0.36
S2-1	60	216.83	156.8	61.88	1.88
S2-2	59	61.06	2.06	59.10	0.1
S2-3	54.00	53.03	0.97	54.11	0.11
S3-1	66.65	69.05	2.40	67.63	0.98
S4-1	84.06	86.06	2.00	83.90	0.16
S5-1	47.62	48.03	0.41	46.17	1.45

The size of the window employed for the moving average filter in the previous experiment is set to one. It means, no moving average is applied to the data obtained from the previous test. Because, the signal is already smooth. But, when it comes to the case where facial expressions and/or head pose are changing, the effect of the moving average becomes more visible. Table 2 shows the results of the proposed system against the work of (Balakrishnan, 2013) and the ground truth. The descriptions of the headings (a)-(f) are the same as those for Table 1. The size of the moving average window changes between 40-80 samples, for different testing scenarios. It can be seen from this table that the proposed system is more robust than the work of (Balakrishnan, 2013) in most of the cases, when the facial expression and/or head pose are changing.

5 CONCLUSIONS

Motivated by the fact that in many applications like, e.g., remote patient monitoring, there is not a possibility for installing a device on the body of the patients, this paper has proposed a contactless

Table 2: Comparing the results of the proposed system against the state-of-the-art work of (Balakrishnan, 2013) when the facial expressions and/or head pose are changing. Please see the text for the descriptions of the headings.

		The test subject is smiling!				The test subject is speaking!			
a	b	c	d	e	f	c	d	e	f
S1-1	66.67	49.051	17.61	58.22	8.45	81.28	14.61	67.31	0.64
S2-1	59	48.02	10.98	59.35	0.35	75.09	16.09	58.41	0.59
S2-2	54.00	56.04	2.04	54.99	0.99	79.05	25.05	52.66	1.34
S3-1	66.65	48.04	18.61	56.77	9.88	51.03	15.62	66.50	0.15
S4-1	84.06	148.09	64.03	61.73	22.33	61.04	23.02	63.78	20.28
S5-1	47.62	47.03	0.59	48.44	0.82	46.72	0.9	48.14	0.52

		The test subject is angry!				The head pose is changing!			
a	b	c	d	e	f	c	d	e	f
S1-1	66.67	50.05	16.62	59.23	7.44	49.03	17.64	60.47	6.2
S2-1	59	63.04	4.04	59.86	0.86	48.02	10.98	59.69	0.69
S2-2	54.00	49.04	4.96	63.96	9.96	50.04	3.96	53.04	0.96
S3-1	66.65	49.05	17.60	59.92	6.73	50.05	16.6	58.87	7.78
S4-1	84.06	63.03	21.03	47.76	36.3	146.10	62.04	57.87	26.19
S5-1	47.62	50.05	2.43	59.23	11.61	51.05	3.43	45.90	1.72

heartbeat rate measurement using computer vision techniques. The system finds some robust feature points inside the facial areas of the users and tracks them over time to generate some trajectories of the feature points. These trajectories are then smoothed by a moving average filter. Then, the irrelevant frequencies are removed from the trajectories. All of these refined trajectories are then fed to a PCA algorithm to find the strongest independent component. This component is assumed to be the estimated heart beat signal. To find the periodicity of this estimated signal a DCT-based algorithm has been used. Experimental results on several video sequences show that the estimated heartbeat rates in different facial expressions and head poses are very close to the ground truth. Furthermore, it is shown that the proposed system outperforms state-of-the-art.

REFERENCES

- Balakrishnan, G., Durand, F. and Guttag, J., 2013, Detecting Pulse from Head Motions in Video. Computer Vision and Pattern Recognition, Proceedings CVPR '13, 2013 IEEE Computer Society Conference on.
- Bouguet, J., 2000, 'Pyramidal implementation of the Lucas Kanade feature tracker', Intel Corporation, Microprocessor Research Labs, Technical Report.
- Hu, S., Zheng, J., Chouliaras, V. and Summers, R., 2008, 'Feasibility of imaging photoplethysmography', in Proceedings of IEEE Conference on Biomedical Engineering and Informatics, pp. 72-75.
- Humphreys, K., Ward, T. and Markham, C., 2007, 'Noncontact simultaneous dual wavelength photoplethysmography: a further step toward noncontact pulse oximetry', Rev. Sci. Instrum., vol. 78, Issue 4, pp. 853-857.
- Poh, M., McDuff, D. and Picard, R., 2010, 'Non-contact, automated cardiac pulse measurements using video imaging and blind source separation', Optic express, Optics Express, Vol. 18, Issue 10, pp.10762-10774.
- Shi, J., Tomasi, C., 'Good features to track,' 1994, Computer Vision and Pattern Recognition, Proceedings CVPR '94., 1994 IEEE Computer Society Conference on, pp.593-600.
- Takano, C. and Ohta, Y., 2007, 'Heart rate measurement based on a time-lapse image', Med. Eng. Phys. Vol. 29, Issue 8, pp. 853-857.
- Verkrusse, W., Svaasand, L. and Nelson, J., 2008, 'Remote plethysmographic imaging using ambient light', Opt. Express, Vol. 16, Issue 26, pp. 21434-21445.
- Viola, P. and Jones, M., 2001, 'Rapid object detection using a boosted cascade of simple features', Computer Vision and Pattern Recognition, , Proceedings CVPR '01., 2001 IEEE Computer Society Conference on, pp. 511-518.
- Wieringa, F., Mastik, F. and van der Steen, A., 2005, 'Contactless multiple wavelength photoplethysmographic imaging: a first step toward "SpO2 camera" technology', Ann. Biomed. Eng. Vol. 33, Issue 8, pp.1034-1041.
- Wu, H., Rubinstein, M., Shih, E., Guttag, J., Durand, F. and Freeman, W., 2012 'Eulerian Video Magnification for Revealing Subtle Changes in the World', ACM Transactions on Graphics, Proceedings SIGGRAPH 2012, Vol. 31, Issue 4, pp. 65-72.